



AN ABRIDGMENT OF IMAGE FILTERING APPROACHES

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Abstract: Given its popularity and growth, image processing is one of the most active research areas. Image processing is the process of turning a physical image into a digital one and apply a variety of procedures to it, such as image enhancement or information extraction. Image filtering is one of the most intriguing uses of image processing. An approach used to manipulate the images' size, shape, colour, depth, smoothness, etc. is called image filtering. In essence, it modifies the image's pixels to give it the intended appearance utilising various graphical editing techniques via graphic design and editing tools. This study provides an introduction to several picture filtering methods and their numerous uses.

Index Terms – Linear Filter, Non-Linear Filter , Thresholding, Sharpening, Smoothing

I. INTRODUCTION

There are primarily two types of algorithms: linear [1] and non-linear [2]. Linear filter can be accomplished through convolution and Fourier multiplication while Non-linear filter is not possible through any of these and its output is not the linear function of its input therefore, its outcome varies in an unintuitive manner. Softening an image reduces noise, for example, and blurred images can be corrected. Fig. 1 shows the classification of image filtering approaches.

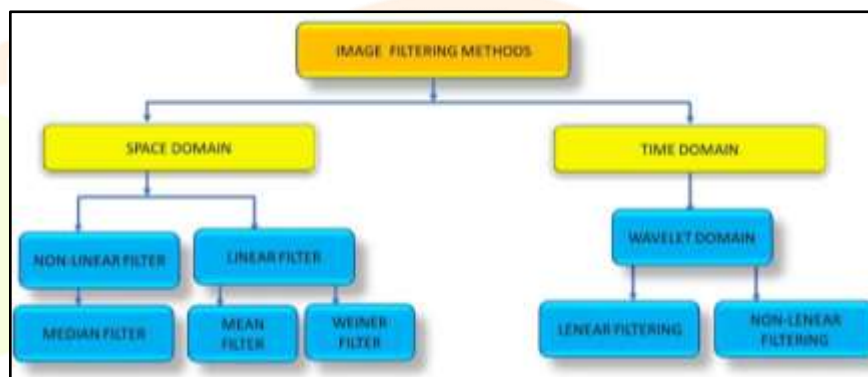


Fig.1: Classification of image filtering approaches

Experts and academics have put forth a variety of approaches for denoising photos, and these techniques have shown decent results. But the majority of techniques, including multiplicative, salt-and-pepper, and Gaussian noise, are used on single noise. Although there are now various ways for removing mixed noise, such as salt and pepper noise with Gaussian noise, the denoising result is not optimal, and there are numerous other fields that merit advancement [3-6]. Gaussian noise and impulse noise make up the majority of the noise in most photos. The two sorts of noise frequently coexist at the same time. Gaussian noise is a byproduct of electronic circuit noise and sensor noise brought on by insufficient lighting or a warm environment. It exhibits great density and a wide range of noise intensity fluctuations [7]. The black and white specks on the image are caused by impulse noise, also known as salt and pepper noise, which is produced by the image sensor, transmission channel, decoder, etc. The key thing to keep in mind when denoising an image is to preserve the integrity of the image's characteristics while reducing noise.

The two primary kinds of conventional filtering methods are spatial domain and frequency domain [8]. Traditional spatial filtering techniques used in the spatial domain method include median, mean, Gaussian, and bilateral filtering. This method processes the image pixels directly. In order to improve the image and achieve the goal of denoising, the frequency domain approach first converts the original image into the frequency domain using integral transformation, then deals with the image in the frequency domain, and

then transforms it into the spatial domain inversely. The Fourier transform, discrete cosine transform, wavelet transform, multi-scale geometric analysis, and other techniques are used in conventional frequency domain filtering.

II. PREVAILING APPROACHES

Standard median filtering is a widely used and efficient technique for removing salt and pepper noise from photos among all the methods for doing so. The technique effectively reduces impulse noise by replacing each pixel's grey value in the original image with the median value of pixels nearby a tiny window. It is possible to better keep the image edge and other characteristics. The algorithm's use of the neighbourhood median to substitute every noise image pixel has the drawback of sharply reducing the algorithm's filtering performance in the presence of high-density noise pollution. It also causes the edges to shift and obscures the texture specifics. A few enhanced median filtering methods [9] have been proposed as a result. These methods can remove salt and pepper noise with high density and enhance the efficiency of median filtering to some extent, but they still fall short in protecting image edge features. The work in [10] is an enhanced Adaptive Median Filter (AMF) technique that can change the filter window's size in response to the noise level, but it is simple to filtering by erroneously considering the extreme point to be a noise point.

Another enhanced adaptive median filtering technique is found in [11]. The algorithm, which is based on the concept of maximum-minimum median filtering, employs a two-level detection technique to precisely separate pixels into signal points and noise points in order to successfully filter out image noise. An enhanced multilayer median filtering technique (VHWR) was suggested in reference. The technique can significantly enhance the filtering impact of salt and pepper noise with high density and keep image details more effectively. However, when the noise density is too high, the denoising impact is insufficient.

The wavelet threshold denoising approach has been widely utilised since Donoho et al. presented the hard threshold function [12] and the soft threshold function [13]. Yet the fixed deviation of the soft threshold function will result in fuzzy or overly smooth boundaries to the denoised image, while the irregularity of the hard threshold functional will lead the rebuilt image's signal to fluctuate. To obtain a more precise denoising impact, many academics have proposed numerous enhanced wavelet threshold values [14]. The wavelet threshold function and threshold are improved by new wavelet threshold technique, which addresses the issues with fixed deviation and discontinuity in the conventional wavelet threshold service.

III. TYPES OF FILTERING

One of the most fundamental processes in image processing, image filtering can significantly enhance image quality and reveal information that would have else been ignored. One should be aware that while some filters are commonly used for smoothing or denoising, others are known for detecting or preserving edges. You should also be aware that filter performance depends on the input image as well as the filtering parameters you choose, like the kernel size, shape, iterations, and interpretations.

The most effective outcomes can occasionally be achieved by using two or more filters in order. For instance, you could need to maintain edges while reducing noise in areas that are homogenous. You may easily combine consecutive filtering processes in the Image Processing panel to make a composite filter. You should be careful to record the order of your operations, though, as some filters can be incompatible and not always be applied sequentially. On each XY-slice of the volume using a 2D kernel or on the entire volume using a 3D kernel, various image filters and image processing algorithms can be applied.

3.1 Artifact Removal

These filters can be used to eliminate stripes from visual data that appear in any direction and in both the vertical and horizontal directions. The destriping filters function by introducing a pattern that disrupts the image to eliminate stripes. To improve the sharpness and get rid of compression-related faults in your image, apply the JPEG artefacts removal filter.

3.2 Comprehensive

Deep learning models that have been trained for tasks like denoising, segmentation, and image enhancement may process picture data using these filters. With the use of deep learning models that have been specially trained for tasks like denoising, segmentation, and image enhancement, picture data can be processed using the comprehensive filters. You should be aware that the Infinite Toolbox (see Infinite Toolbox) offers a variety of trained and untrained deep learning models for download. Before users may access the thorough filters, you must download or generate at least one model.

3.3 Contrast Adjustment

By revising the grayscale or the picture's range of values, these filters can be used to change the contrast in photographs. A computer image processing method called adaptive histogram equalisation (AHE) is used to enhance contrast in photographs. The adaptive approach is different from traditional histogram equalisation in that it computes many histograms, each corresponding to a different area of the image, and then utilises them to disperse the image's brightness values. Therefore, it is appropriate for strengthening the definition of edges in each area of an image as well as the local contrast. AHE has a propensity to exaggerate noise in relatively homogeneous areas of an image, though. This is avoided by contrast limited adaptive histogram equalisation (CLAHE), a type of adaptive histogram equalisation, by restricting the amplification. The contrast limiting approach is used in the case of CLAHE for each neighbourhood where a transformation is made[15].

Histogram equalisation is a contrast enhancing technique that remaps the grey scale so that the resulting image makes use of the entire range and has roughly the same proportion of pixels for each grey value. A nearly linear cumulative distribution function characterises the equalised image. The efficiency of employing the same amount of pixels for each grey value must be determined empirically, it should be noted. You should be aware that this process has the potential to remap vast homogeneous regions into more grey levels. It's possible that this will aid in visual interpretation. While histogram equalisation has the benefit of requiring no parameters, it occasionally produces photos that don't look natural. Local histogram equalisation is an alternate technique.

3.4 Detector

These filters draw attention to an image's edges and transitions. In volumetric imaging data, the Frangi filter is commonly used to identify vessels, tubes, and fibres. In an image, the Hessian filter looks for continuous edges. This filter uses an alternative approach of smoothing and is almost as good as the Frangi filter.

3.5 Edge Detection

These filters draw attention to an image's edges and transitions. variance between gaussian applies a Gaussian blur to a picture with a first sigma value that is supplied. The final image is a distorted version of the original. The module then applies a second blur (second sigma), which blurs the image less than the first blur. The difference between the two blurred images is then used to replace each pixel in the final image, and the values are monitored for when they pass zero. The edges or regions of pixels that have some variance in their immediate neighbourhood will be the focus of the resulting zero crossings.

The Laplacian filter highlights the areas where there is a sudden intensity change by employing an isolated convolution kernel that roughly approximates the second derivatives of the image in the definition of the Laplacian. This filter can be used to emphasise the edges in a picture. Any brightness slope, positive or negative, is amplified by the Laplacian enhancement procedure, which creates prominent peaks at the edges. Prewitt utilises the Prewitt transform to identify an image's horizontal and/or vertical edges.

3.6 Editable Detection

It combines an image with a personalised 2D or 3D kernel, allowing you to generate filter effects like boosting, amplifying, sharpening, and smoothing.

3.7 Frequency Domain

For converting time domain signals to frequency domain signals and for inverting modified signals, two filters—discrete Fourier transform and inverse discrete Fourier transform—are offered. With no information lost, the discrete Fourier transform (DFT) converts a signal from the so-called time domain, where each sample in the signal is linked to a specific time, into a collection of values in the frequency domain, where each value is a complex integer linked to a certain frequency. The magnitude, phase, real (even), and imaginary (odd) components of the transform are all outcomes of the DFT. The complex frequency series is translated back into the original time series using the Inverse Discrete Fourier Transform (IDFT). The IDFT will produce complex numbers with a zero-valued imaginary portion if the initial time series was made up of real values. The magnitude and phase data are the IDFT's essential inputs.

3.8 Morphology

Picture filtering can be used to increase or reduce picture regions, as well as to remove or fill-in image region boundary pixels. Morphological operators include dilate, erode, open, and close.

Basic mathematical morphology operators include dilation and erosion. The primary result of dilation on a picture is a gradually expanding border around foreground pixel regions, which are often white pixels. Holes within foreground pixel regions get smaller as those regions get bigger. The primary impact of erosion on an image is the erosion away of the edges of foreground pixel regions, which are often white pixels. Holes within foreground pixel areas get larger as those areas' size decreases.

Edge detection is another application of dilation, which highlights only the additional pixels that the dilation added to the edges of objects by subtracting the original picture from the dilation of an image. Similar to how it can be used for edge detection, erosion can be applied on an image and then subtracted from the original. This will draw attention to only the pixels at the margins of items that the erosion has eroded away. The image to be dilated or eroded and a set of coordinate points known as a structuring element or kernel are the two pieces of data that the dilation and erosion operator accepts as inputs. This structural component affects how precisely erosion or dilation will affect the input image.

The basic morphological processes of erosion and dilation give rise to opening. Opening generally tends to remove part of the foreground (bright) pixels from the margins of regions of foreground pixels, similar to how erosion tends to do. It generally causes less damage than erosion. Similar to other morphological operators, a structural factor determines the precise operation. The operator has the effect of removing all other foreground pixel regions while preserving foreground regions that are similar in shape to the structuring element or that can entirely enclose the structuring element.

The definition of closing is just a dilation followed by an erosion using the same structural element for both operations. Closing is opening done backwards. In that it tends to extend the borders of foreground (bright) regions in an image and fill-in tiny background holes known as pepper noise, closing is similar to dilation in certain ways. It frequently causes less damage to the original boundary

shape, nevertheless. Similar to other morphological operators, a structural factor determines the precise operation. The operator has the effect of removing all other regions of background pixels while preserving background regions that are similar in shape to this structuring element or that can entirely enclose the structuring element.

The top-hat transform is an operation used in mathematical morphology and digital image processing to extract minute details and elements from provided images. The white top-hat transform and the black top-hat transform are the two different sorts of top-hat transforms. The black top-hat transform can be described as the difference between the input image and the closing, and the white top-hat transform can be described as the difference between the input image and its opening by some structuring element. For a variety of image processing applications, including feature extraction, background equalisation, image enhancement, and others, top-hat transforms can be utilised.

The result of white top-hat filtering is an image with objects or elements from the input image that are both smaller and brighter than the structuring element. The result of white top-hat filtering is an image with objects or elements from the input image that are both smaller and brighter than the structuring element.

A morphological gradient in digital image processing is the distinction between an image's erosion and dilatation. When the Morphological Gradient filter is used, the result is an image where each pixel value represents the level of contrast in its immediate surroundings. Applications for edge detection and segmentation may benefit from this.

3.9 Segmentation

K-Means and Mini-Batch K-Means are two filters that can be used to divide an image into a set number of relevant sections.

By attempting to divide samples into n groups with identical variance and minimising the inertia or within-cluster sum-of-squares criterion, one can group data. The number of clusters must be given for this algorithm.

The Mini-Batch K-Means option is a K-Means algorithm version that still seeks to optimise the same objective function while using mini-batches to speed up calculation times. In each training cycle, mini-batches, which are subsets of the input data, are randomly sampled. Mini-Batch K-Means generates results that are typically just marginally worse than the conventional algorithm, in contrast to other techniques that speed up K-Means' convergence.

3.10 Shading compensation

These filters can be utilised to eliminate unwanted field-of-view shading, a significant microscopy phenomenon that can be brought on by uneven lighting, uneven detector sensitivity, or non-specific sample staining. The shading compensation filters can substantially reduce unwanted shading across the field of view, which can be a notable occurrence in microscopy and may be caused by uneven lighting, uneven detector sensitivity, or non-specific sample staining. For later processing, it is frequently required to remove shading, especially when quantification is the end aim. The intensity profile of rulers drawn across a picture can be used to identify when a dataset needs to be corrected for shading. If linear regression is evident, as is demonstrated in the example below, shade removal may be necessary.

Balancing the histogram spreads out the image's most prevalent intensity levels. A nearly linear cumulative distribution function characterises the equalised image.

It concurs with a number of observations—chiefly the fact that non-degraded images typically have very low entropy in comparison to their degraded counterparts and that degradations make pixel values less predictable from values in their neighborhoods—to reduce randomness in order to correct for non-uniform illumination and combat noise. You should be aware that while though entropy reduction normally has a much greater impact on random degradations than the signal, it may eventually destroy much of the source image's natural diversity.

RBF manually This filter uses a radial basis function to fix image shading issues that are typically caused by non-uniform illumination. You should be aware that the Manual RBF filter only applies corrections in the X and Y axes and that at least three (3) seed points must be put in representative areas on an image slice. You must change the data if corrections in a different direction are necessary.

3.11 Sharpening

When post-processing many different types of photographs, sharpening is essential since it can assist highlight details and improve the edges of objects in a picture. When sharpening an image, you should be aware of the following: Sharpening should be the final step in a filtering pipeline because it is particularly output-specific. Sharpening filters are extremely noise-sensitive. If necessary, noise reduction should always be used first. For optimum results, the right radius must be selected because sharpening might produce undesirable edge effects or increase image noise.

The functions of the Gaussian High Pass filter and the Gaussian filter are the exact opposite. The Gaussian High get filter filters low frequency picture information while allowing high frequency image information to get through. The image is effectively sharpened by this. The Gaussian filter, in contrast, is a low pass filter that only lets low frequency picture data through while blocking high frequency image data. This successfully smoothes or blurs the image.

Contrary to what its name might imply, the Unsharp filter, also known as an unsharp mask filter, is used to sharpen an image. As a result, it is a very flexible tool that may sharpen edges that are blurry in the original image and enhance the definition of tiny detail.

The ability to regulate the sharpening process is one of the Unsharp filter's main advantages over other sharpening filters. Many sharpening filters don't offer any programmable settings.

The unsharp mask, a slightly blurred copy of the original image, is the first step in the sharpening process. In order to find edges, this is removed from the original image. Using this mask, contrast is then selectively enhanced along these edges, leaving behind a sharp image.

3.12 Smoothing

To lessen the amount of noise in an image, image smoothing filters such as the Gaussian, Maximum, Mean, Median, Minimum, Non-Local Means, Percentile, and Rank filters can be used. One should be aware that even while these filters are excellent in reducing noise, they must be applied carefully to avoid changing the image's crucial information. It's also important to keep in mind that, in many situations, smoothing should come before edge detection or augmentation.

The Gaussian filter blurs an image and eliminates noise and detail in the process. It is comparable to the Mean filter in this regard. It does, however, employ a kernel that mimics a Gaussian or bell-shaped hump. The Gaussian filter produces a weighted average of each pixel's neighbourhood, with the average leaning more heavily towards the value of the centre pixels than the Mean filter's equally weighted average. As a result, compared to a Mean filter of comparable size, the Gaussian filter offers a softer smoothing and better maintains edges. The frequency response of the Gaussian filter is one of the main arguments in favour of employing it for smoothing. Lowpass frequency filters are what the majority of convolution-based smoothing filters do. This indicates that their impact on an image is to eliminate high spatial frequency components. The range of spatial frequencies present in the image after filtering may be reasonably predicted by selecting an adequately sized Gaussian, which is not the case with the Mean filter. Computational biologists are also paying attention to the Gaussian filter since some biological plausibility has been attached to it. For instance, some brain cells involved in the visual circuits frequently exhibit a roughly Gaussian response.

Mean filtering is a straightforward technique for reducing noise in photos and smoothing out pixel values that aren't accurate representations of their surroundings. With mean filtering, each pixel's value in an image is changed to the mean or average of its surrounding pixels, including itself.

The Mean filter, like other convolutional filters, is built around a kernel that symbolises the form and size of the neighbourhood to be sampled when determining the mean. Although larger kernels might be used for smoothing that is more severe, a 3x3 square kernel is frequently employed. It should be noted that a small kernel can be used multiple times to achieve a result that is similar to, but not exactly the same as, a single pass with a large kernel. Although noise is less noticeable after mean filtering, the image has been softened or blurred and high frequency detail has been lost. This typically happens as a result of the filter's following shortcomings:

The mean value of all the pixels in a given area might be greatly impacted by a single pixel with a highly unrepresentative value. The filter will interpolate new values for pixels on the edge when the filter neighbourhood crosses an edge. If the output needs sharp edges, this could be a problem.

The Median filter, which is more frequently employed than the Mean filter for noise reduction, can address both of these issues. Other convolution filters that do not determine a neighborhood's mean are also frequently used.

Mean shift filtering depends on a data clustering approach that is frequently employed in image processing and can be utilised for edge-preserving smoothing. The set of adjacent pixels is established for each image pixel with a specific grayscale value and spatial location. The new spatial centre (spatial mean) and the new mean value are computed for this group of neighbouring pixels. The new centre for the following iteration is then determined by these estimated mean values. The given technique will be repeated until there is no longer any change in the spatial and grayscale means. The final mean value will be applied to the iteration's beginning location at the conclusion of the iteration.

The Median filter is frequently more effective at maintaining detail and edges in an image than the Mean filter when used to reduce noise in an image. Similar to the Mean filter, this filter evaluates the representativeness of each pixel in turn by examining its neighbours in the immediate vicinity. However, it replaces the pixel value with the median of those values rather than just the mean of the pixels next to it. For the purpose of reducing the random intensity spikes that frequently appear in images taken with microscopes, median filters are very helpful.

The Median filter has two key advantages over the Mean filter since it determines a neighborhood's median value rather than its mean value: A single, incredibly unrepresentative pixel in a neighbourhood won't have a major impact on the median value since the median is more robust than the mean. For instance, in datasets that feature salt-and-pepper noise (scatter dots) contamination. The Median filter does not produce irrational pixel values when it crosses an edge since the median value must actually be the value of one of the pixels in the neighbourhood. Because of this, it preserves sharp edges far better than the Mean filter. The Median filter, yet, isn't always as effective as the Mean filter in handling significant levels of Gaussian noise. It is also fairly difficult to compute.

The Non-Local Means filter takes the mean of all pixels in the image, weighted by how similar they are to the target pixel, as opposed to the Mean filter, which takes the mean value of a set of pixels around a target pixel to smooth an image. When compared to mean filtering, applying this filter can produce improved post-filtering clarity with no loss of detail. The Non-Local Means or Bilateral filter should frequently be your first option for reducing noise in photos. One should be aware that non-local means filtering performs best when the data's noise is white noise, in which case the majority of the image's features, including thin and small ones, will be kept. Fig. 2 illustrates classification of smoothing and sharpening filters.

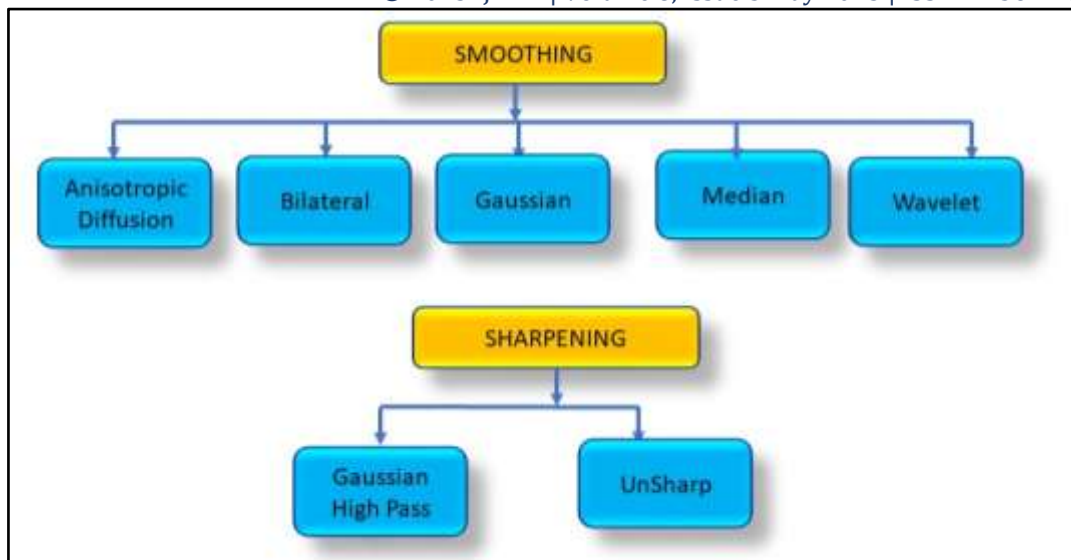


Fig. 2 Classification of smoothing and sharpening filters.

3.13 Texture Analysis

By measuring the spatial variation in pixel intensities, texture analysis describes the texture of a given area. Gabor uses oriented patterns to divide items. Elements are divided by Image Moments using various textures. Elements with various textures are separated by a local binary pattern. Through directed filtering, Membrane Projections amplifies an image's membrane-like features.

3.14 Thresholding

Thresholding filters provide an image divided into the foreground and background, two fundamental classes. For segmentation or other image analysis tasks, these images can be used as masks. Adaptive Apply an adaptive threshold to a set of elements. Bring back the threshold value(s) using the ISODATA technique. In other words, threshold intensities that divide a picture into two groups of pixels and are returned are intensities that are halfway between the mean intensities of these groups. LI Based on a modification of Li's Minimum Cross Entropy approach, return the threshold value. Yen returns threshold value based on Yen's method.

The OTSU filter outputs an image that is divided into two fundamental classes—foreground and background—and is an adaptation of the Otsu thresholding technique. The ideal value that minimises the weighted within class variances of these two classes is calculated in this thresholding procedure. You should be aware that maximising the between class variation and minimising the within class variance are equivalent. The quickness of the Otsu thresholding method is one of its key benefits, whereas the method relies solely on uniform lighting and disregards both spatial coherence and object framework. One should examine the image histogram before using this filter because Otsu thresholding operates on histograms. Examine Using Histograms. Fig. 3 illustrates the details of filtering algorithms.

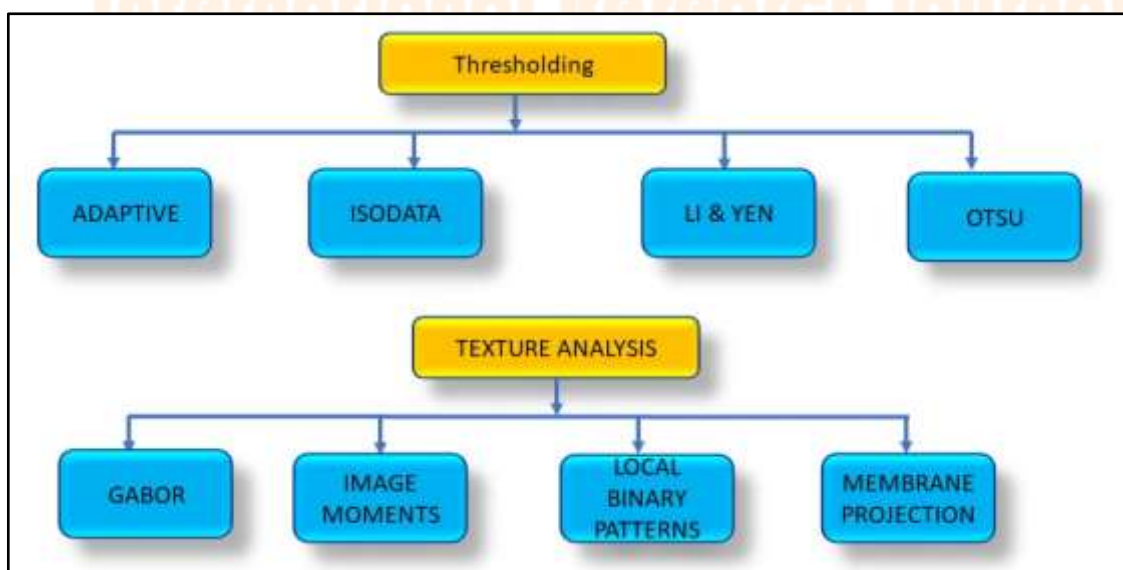


Fig. 3: Detailed classification of Filters

V. CONCLUSION

Edge detection, noise reduction, sharpening, and smoothing are just a few of the many uses for image filtering. The discipline of image processing has undergone an evolutionary transition thanks to image filtering. A kernel, which is a tiny array applied to each pixel and its immediate neighbours in the given image, can be thought of as the basic unit of a filter. This study compares various

techniques and provides a quick explanation of picture filtering. We have also briefly addressed some of its many applications, including denoising, image enhancement, compression, and restoration. Median and bilateral filters are suggested when noise reduction is required while still keeping the image's peaks and edges. However, if only the image's peaks need to be maintained and the edge effect is unimportant, the gaussian filter is sufficient because it requires relatively less computation. Box filter will be enough if the primary goal is noise reduction and peaks and edges are not taken into account.

REFERENCES

- [1] Thomas Kailath. 1974. A view of three decades of linear filtering theory. *IEEE Transactions on information theory*, 20(2):146–181.
- [2] Pia Addabbo, Filippo Biondi, Carmine Clemente, Danilo Orlando, and Luca Pallotta. 2019. Classification of covariance matrix eigenvalues in polarimetric sar for environmental monitoring applications. *IEEE Aerospace and Electronic Systems Magazine*.
- [3] Akash D., Princy, Kirti B., Rohini S. 2022. Demosaicing Techniques Thorough Analysis. *International Journal of Innovative Research in Science, Engineering and Technology*, 11(7), 9902-9907.
- [4] Akash D., Princy, Kirti B., Rohini S. 2022. Development of Soma-based Demosaicing. *International Journal of Advanced Research in Electrical, Electronics and Instrumentation Engineering*. 11(7): 2795-2799.
- [5] Mahesh K. , Kirti B., S. Bhadola, Rohini S. 2022. An Image Sharpening and Smoothing Approaches Analysis. *International Journal of Innovative Research in Computer and Communication Engineering*. 10(6), 5573-5580.
- [6] Mahesh K. , Kirti B., S. Bhadola, Rohini S. 2022. Development of a fourier transformation based model for image smoothing. *International Research Journal of Modernization in Engineering Technology and Science* . 4(6): 4204-4210.
- [7] Shrestha, S. 2014. Image denoising using new adaptive based median filters. *Signal Image Process*. 5, 1–13.
- [8] Jeevan, K.M.; Krishnakumar, S. 2018. An algorithm for wavelet thresholding based image denoising by representing images in hexagonal lattice. *J. Appl. Res. Technol*. 16, 103–114.
- [9] Roy, A.; Singha, J.; Manam, L.; Laskar, R.H. 2017. Combination of adaptive vector median filter and weighted mean filter for removal of high-density impulse noise from color images. *IET Image Process*. 11, 352–361.
- [10] Hwang, H.; Haddad, R. 1995. Adaptive median filters: New algorithms and results. *IEEE Trans. Image Process*. 4, 499–502.
- [11] Huang, B.G.; Lu, Z.T.; Ma, C.M. 2011. Improved adaptive median filtering algorithm. *J. Comput. Appl*. 7, 1835–1837.
- [12] Donoho, D.L.; Johnstone, I.M. 1994. Ideal spatial adaptation via wavelet shrinkage. *Biometrika*. 81, 425–455.
- [13] Donoho, D.L. 1995. Denoising by soft-thresholding. *IEEE Trans. Inf. Theory*. 41, 613–627.
- [14] Wang, Q.; Cheng, B.; Du, J.; Xu, G. 2015. An improved method for image denoising based on wavelet thresholding. *Comput. Mod*. 4, 65–69.
- [15] http://www.theobjects.com/dragonfly/dfhelp/Content/05_Image%20Processing/Image%20Filters%20and%20Settings.htm.

