



SECURE OUTSOURCING OF NON-LINEAR OPTIMIZATION IN CLOUD COMPUTING

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ABSTRACT

Non-linear programming is generally very difficult to find an approximate solution NLP problem. Security is the primary barrier, mainly for customers for their data are exhaust and yield during computing. This researches secure outsourcing of non-linear programming computing. By validating the result explore the NLP computing and derive the sufficient conditions that result must satisfy. MATLAB Programming to Non-linear programming problem by Golden Section Search Method.

Key Words: NLP problems, Cloud computing, MATLAB, Golden Section Method.

1.1 INTRODUCTION TO CLOUD COMPUTING:

Cloud computing often refer to as the “cloud” is a server. Cloud computing refers to on- demand internet access to computing resources such as program, service, data storage, development tools, networking capabilities, etc. that are placed at a remote data center. Cloud computing means storing and accessing data, files and programs over the internet. The cloud environment provides an easily accessible online portal that makes handy for the user to manage the compute, storage, network, and application resources.

1.2 NON-LINEAR PROGRAMMING:

A Non-linear programming is a process of solving an optimization problem where the objective function or the constraints are non-linear. Non-linear programming is the general form of linear programming problem, except the objective functions but the constraints may be linear or non-linear terms. Non-linear programming is a mathematical technique for finding an optimal solution. Non-linear programming are non-linear equations because the decision variables in the objective function having the degree more than one. Several methods have developed for solving non-linear programming problems. Non-linear programming is to calculate the maxima, minima or the stationary points of an objective function of unknown decision variables and conditional to satisfactions of a system of equality and inequality constraints. Non-linear programming is also known as the non-linear optimization.

1.3 GENERAL FORM OF NON-LINEAR PROGRAMMING:

Let z be a real valued objective function of n variables defined by: Optimize (max or min) $z = f(x_1, x_2, \dots, x_n)$
Let (b_1, b_2, \dots, b_m) be a set of constraints, such that:

$$g_1(x_1, x_2, \dots, x_n) \quad [\leq \text{ or } \geq \text{ or } =] b_1$$

$$g_2(x_1, x_2, \dots, x_n) \quad [\leq \text{ or } \geq \text{ or } =] b_2$$

$$g_3(x_1, x_2, \dots, x_n) \quad [\leq \text{ or } \geq \text{ or } =] b_3$$

$$g(x_1, x_2, \dots, x_n) \quad [\leq \text{ or } \geq \text{ or } =] b_m$$

Where , $g_1(x_1, x_2, \dots, x_n) \quad [\leq \text{ or } \geq \text{ or } =] b_1, \dots, g_m(x_1, x_2, \dots, x_n) \quad [\leq \text{ or } \geq \text{ or } =] b_m$ are structural constraints. Let $j \geq 0$ where $j = 1, 2, \dots, n$ be a non-negative constraint.

2. GOLDEN SECTION SEARCH METHOD

2.1 GOLDEN SECTION SEARCH METHOD:

Golden section search method is a technique to find out the extremum (maximum or minimum) for a strictly unimodal function constrict the range of values. The golden section search method is efficient way to progressively reduce the interval locating the minimum/maximum. This method is for minimising a unimodal function over interval $[a, b]$.

Consider a function $f(x)$

Max $f(x)$

Subject to $a \leq x \leq b$

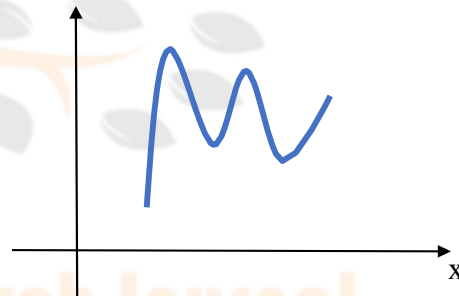
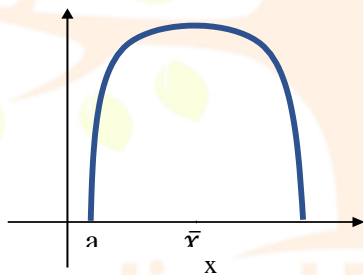
2.1 UNIMODAL FUNCTION:

The function which has either only a minimum or maximum in a particular $[a, b]$. a function $f(x)$ is a unimodal on $[a, b]$ if for some \bar{x} on $[a, b]$, $f(x)$ is strictly increasing on $[a, \bar{x}]$ and strictly decreasing on $[\bar{x}, b]$.

Let \bar{x} denotes the optimal solution.

$f(x)$

$f(x)$



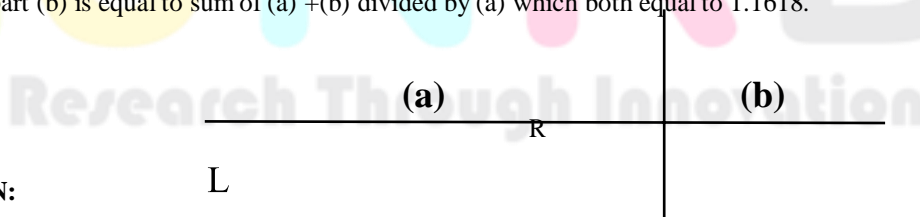
A unimodal function on $[a, b]$

\bar{x} = local maximum

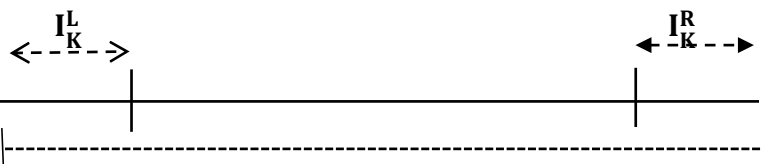
Not a unimodal on $[a, b]$

2.3 GOLDEN RATIO:

The golden ratio is also known as golden section, golden mean, divine proportion or Greekletter phi (ϕ) exists when line is divided into two parts and the longer part (a) divided by the smaller part (b) is equal to sum of (a) +(b) divided by (a) which both equal to 1.1618.



NOTATION:



IK

- $IK = R - L$ Length of the search interval of k^{th} iteration.
- $I^L = x_{1,k} - x_{2,k}$ Length of the left part of the section interval IK .
- $I^R = R - x_{2,k}$ Length of the right part of the search interval IK .

2.4 DERIVATION OF GOLDEN RATIO:

How to choose x_1 and x_2

Choose two points x_1 and x_2 in between the L and R according to the following rule:

1) $I_k^L = I_k^R$, for all k

2) Only point either x_1 or x_2 is computed For instance

$x_{1,k+1} \leftarrow x_{2,k}$ and $x_{2,k+1}$ is computed for I_{k+1}^R

$x_{2,k+1} \leftarrow x_{1,k}$ and $x_{1,k+1}$ is computed for I_{k+1}^L

such that $I_k = I_{k+1} + I_{k+2}$, for all k

3) $\frac{I_k}{I_{k+1}} = \frac{I_{k+1}}{I_{k+2}} = c$ (constant) for all k.

Since $I_{k+1} = I_{k+2}$

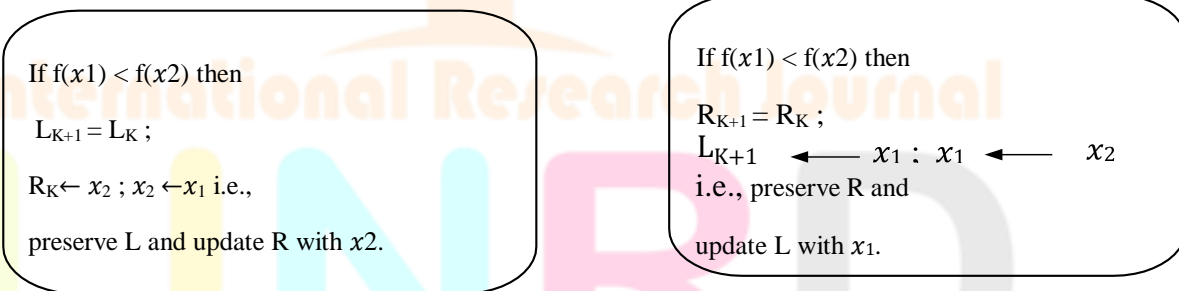
This is called Golden section criterion.

2.5 GOLDEN SECTION RULE ALGORITHM:

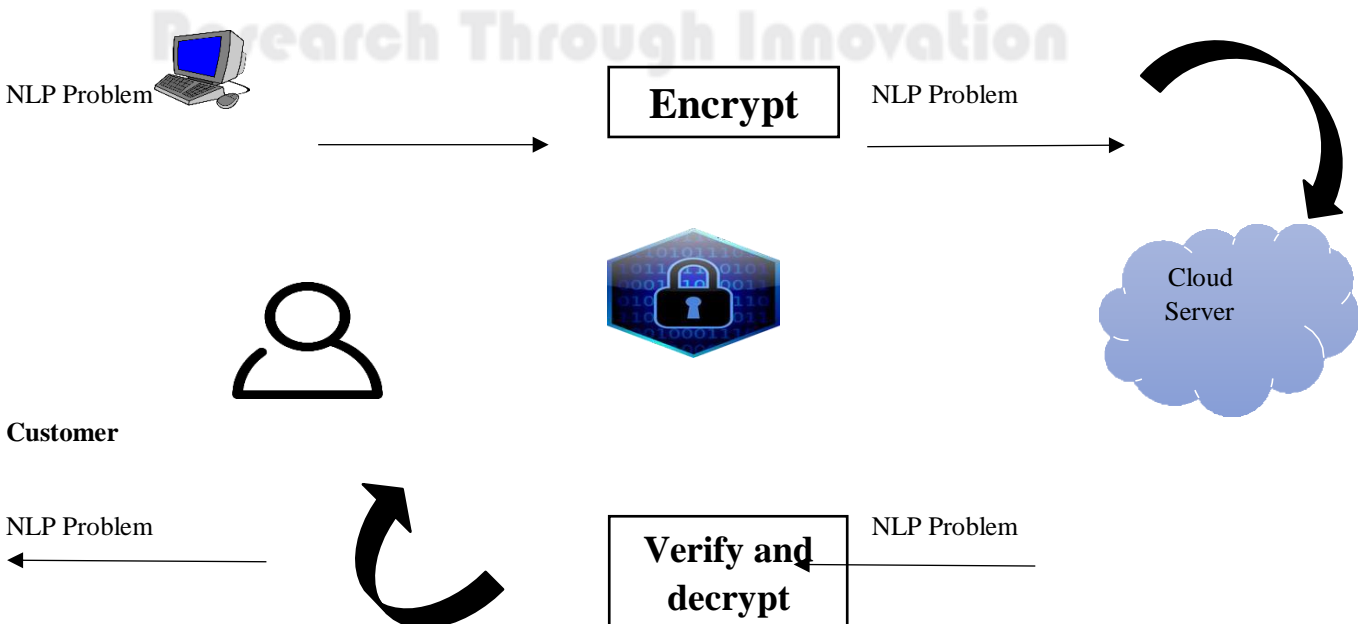
Let initial interval [a, b] be given and the number of iterations be n or tolerance error ϵ

- 1) Set $l = a, R = b; k = 1$ (iteration number)
- 2) Compute x_1 or x_2 as
 $x_2 = L + 0.618(R - L)$ and
 $x_1 = L + R - x_2$
 Repeat step 2 until requirement met.

3. PROPOSED SYSTEM:



A Non-Linear Programming outsourcing scheme which provides a complete outsourcing solution for the privacy protection of problem as well as both input and output. It starts from an overview of secure NLP outsourcing in cloud private data owned by the customer.



3.SOLVING PROBLEM BY GOLDEN SECTION SEARCH METHOD**PROBLEM:**

Perform 6 iterations of the Golden section search method to minimize

$f(x) = \left\{ x^2, \frac{1-x}{2} \right\}$ over $[-1, 1]$ and hence identify the final interval I_6

SOLUTION:

$$\text{Minimize } f(x) = \begin{cases} \frac{1-x}{2}, & x < 0 \\ x^2, & x \geq 0 \end{cases} \text{ over } [-1,1]$$

ITERATION 1:

$X_2 = L + 0.618 (R - L)$ Here $L = -1, R = 1$

$$X_2 = -1 + 0.618 (1 - (-1))$$

$$= -1 + 0.618 (2)$$

$$= -1 + 1.236$$

$$X_2 = 0.236$$

$$X_1 = L + R - X_2$$

$$= -1 + 1 - 0.236$$

$$X_1 = -0.236$$

$$f(x_1) = \frac{1-x}{2}$$

$$= \frac{1 - (-0.236)}{2}$$

$$= \frac{1 + 0.236}{2}$$

$$= \frac{1.236}{2}$$

$$= 0.618$$

$$= 0.618$$

$$= 0.618$$

$$f(x_2) = \frac{1-x}{2}$$

$$= \frac{1 - 0.236}{2}$$

$$= \frac{0.764}{2}$$

$$= 0.382$$

$$= 0.382$$

$$= 0.382$$

$$= 0.382$$

ITERATION 2:

$X_2 = L + 0.618 (R - L)$ Here $L = -0.236, R = 1$

$$X_2 = -0.236 + 0.618 (1 - (-0.236))$$

$$= -0.236 + 0.618 (1 + 0.236)$$

$$= -0.236 + 0.618 (1.236)$$

$$= -0.236 + 0.7638$$

$$X_2 = 0.528$$

$$X_1 = L + R - X_2$$

$$= -0.236 + 1 - 0.528$$

$$= 1 - 0.764$$

$$X_1 = 0.236$$

$$f(x_1) = \frac{1-x}{2}$$

$$= \frac{1 - 0.236}{2}$$

$$= \frac{0.764}{2}$$

$$= 0.382$$

$$= 0.382$$

$$= 0.382$$

$$= 0.382$$

$$f(x_2) = x^2$$

$$= (0.528)^2$$

$$= 0.27878$$

ITERATION 3:

$$X_2 = L + 0.618(R - L) \text{ Here } L = 0.236, R = 1$$

$$X_2 = 0.236 + 0.618(1 - 0.236)$$

$$= 0.236 + 0.618(0.764)$$

$$= 0.236 + 0.4721$$

$$X_2 = 0.708$$

$$X_1 = L + R - X_2$$

$$= 0.236 + 1 - 0.708$$

$$= 1.236 - 0.708$$

$$X_1 = 0.528$$

$$f(x_1) = x^2$$

$$= (0.528)^2$$

$$= 0.27878$$

$$f(x_2) = x^2$$

$$= (0.708)^2$$

$$= 0.50126$$

ITERATION 4:

$$X_2 = L + 0.618(R - L) \text{ Here } L = 0.236, R = 0.708$$

$$X_2 = 0.236 + 0.618(0.708 - 0.236)$$

$$= 0.236 + 0.618(0.472)$$

$$= 0.236 + 0.2916$$

$$X_2 = 0.528$$

$$X_1 = L + R - X_2$$

$$= 0.236 + 0.708 - 0.528$$

$$= 0.944 - 0.528$$

$$X_1 = 0.416$$

$$f(x_1) = \frac{1-x}{2}$$

$$= \frac{1-0.416}{2}$$

$$= \frac{0.584}{2}$$

$$= 0.292$$

$$f(x_2) = x^2$$

$$= (0.528)^2$$

$$= 0.27878$$

$$= 0.27878$$

$$= 0.27878$$

$$= 0.27878$$

$$= 0.27878$$

ITERATION 5:

$$X_2 = L + 0.618(R - L) \text{ Here } L = 0.416, R = 0.708$$

$$X_2 = 0.416 + 0.618(0.708 - 0.416)$$

$$= 0.416 + 0.618(0.292)$$

$$= 0.416 + 0.1804$$

$$X_2 = 0.596$$

$$X_1 = L + R - X_2$$

$$= 0.416 + 0.708 - 0.596$$

$$= 1.124 - 0.596$$

$$X_1 = 0.528$$

$$f(x_1) = x^2$$

$$= (0.528)^2$$

$$= 0.27878$$

$$f(x_2) = x^2$$

$$= (0.596)^2$$

$$= 0.35522$$

ITERATION 6:

$$X_2 = L + 0.618(R - L) \text{ Here } L = 0.416, R = 0.596$$

$$X_2 = 0.416 + 0.618(0.596 - 0.416)$$

$$= 0.416 + 0.618(0.18)$$

$$= 0.416 + 0.1112$$

$$X_2 = 0.528$$

$$X_1 = L + R - X_2$$

$$= 0.416 + 0.596 - 0.528$$

$$= 1.012 - 0.528$$

$$X_1 = 0.484$$



$$f(x_1) = \frac{1-x}{2}$$

$$= \frac{1-0.484}{2}$$

$$= \frac{0.516}{2}$$

$$= 0.258$$

$$f(x_2) = x^2$$

$$= (0.528)^2$$

$$= 0.27878$$

K	L	R	x_1	x_2	$f(x_1)$	$f(x_2)$	L/R
1	-1	1	-0.236	0.236	0.618	0.382	R
2	-0.236	1	0.236	0.528	0.382	0.27878	R
3	0.236	1	0.528	0.708	0.27878	0.50126	L
4	0.236	0.708	0.416	0.528	0.292	0.27878	R
5	0.416	0.708	0.528	0.596	0.27878	0.35522	L
6	0.416	0.596	0.484	0.528	0.258	0.27878	

Thus, $x_{\min} \in [0.416, 0.596]$

Hence, $x^* = \frac{0.416+0.596}{2}$

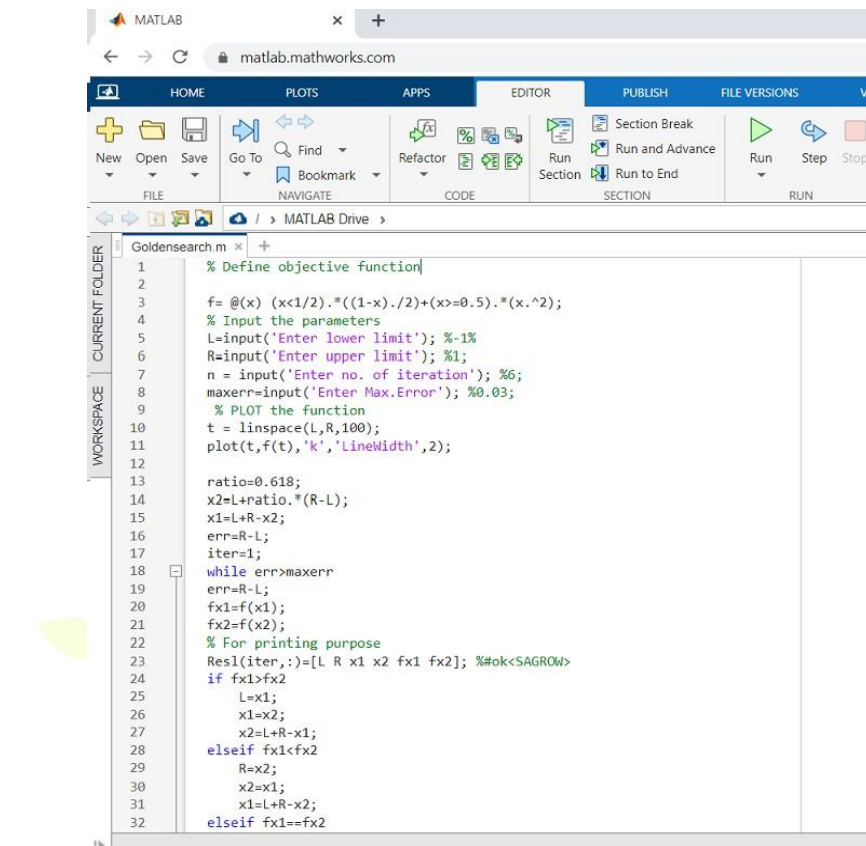
Therefore, Min $f(x^*) = 0.2640$

MATLAB CODING FOR GOLDEN SECTION SEARCH METHOD:

% Define objective function

```
f=@(x)(x<1/2).*((1-x)/2)+(x>=0.5).*(x.^2);
% Input the parameters L=input('Enter lower limit'); % -1 % R=input('Enter upper limit'); % 1;
n = input('Enter no. of iteration'); % 6; maxerr=input('Enter Max.Error'); % 0.03;
% PLOT the function = linspace(L,R,100);
plot(t,f(t),'k','LineWidth',2);

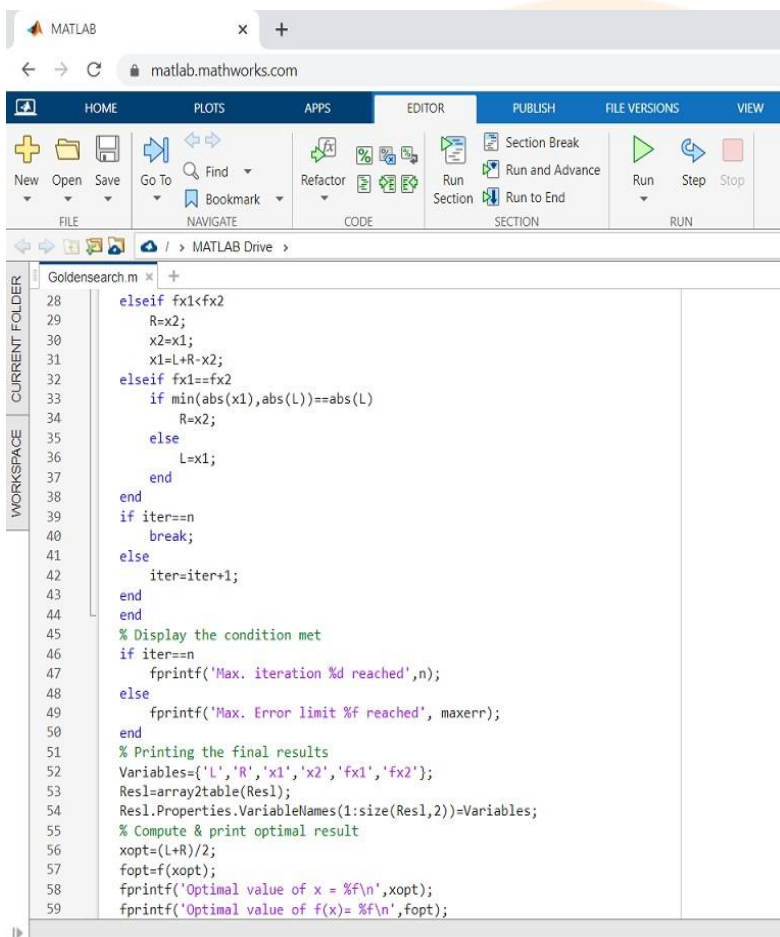
ratio=0.618; x2=L+ratio.*(R-L);x1=L+R-x2;
err=R-L;iter=1;
while err>maxerrerr=R-L; fx1=f(x1); fx2=f(x2);
% For printing purpose
Resl(iter,:)= [L R x1 x2 fx1 fx2]; % #ok<SAGROW>if fx1>fx2
L=x1;
x1=x2; x2=L+R-x1;
elseif fx1<fx2R=x2;
x2=x1; x1=L+R-x2;
elseif fx1==fx2
if min(abs(x1),abs(L))==abs(L)R=x2;
else
L=x1;
endend
if iter==nbreak;
else
iter=iter+1;end
end
% Display the condition met if iter==n
fprintf('Max. iteration %d reached',n);else
fprintf('Max. Error limit %f reached', maxerr);end
% Printing the final results Variables={'L','R','x1','x2','fx1','fx2'}; Resl=array2table(Resl);
Resl.Properties.VariableNames(1:size(Resl,2))=Variables;
% Compute & print optimal result xopt=(L+R)/2;
fopt=f(xopt);
fprintf('Optimal value of x = %f\n',xopt); fprintf('Optimal value of f(x)= %f\n',fopt)
```



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Goldensearch.m
1 % Define objective function
2
3 f=@(x) (x<1/2).*((1-x)/2)+(x>=0.5).*(x.^2);
4 % Input the parameters
5 L=input('Enter lower limit'); %1
6 R=input('Enter upper limit'); %1;
7 n = input('Enter no. of iteration'); %6;
8 maxerr=input('Enter Max.Error'); %0.03;
9 % PLOT the function
10 t = linspace(L,R,100);
11 plot(t,f(t),'k','LineWidth',2);
12
13 ratio=0.618;
14 x2=L+ratio.*(R-L);
15 x1=L+R-x2;
16 err=R-L;
17 iter=1;
18 while err>maxerr
19 err=R-L;
20 fx1=f(x1);
21 fx2=f(x2);
22 % For printing purpose
23 Res1(iter,:)= [L R x1 x2 fx1 fx2]; %#ok<SAGROW>
24 if fx1>fx2
25 L=x1;
26 x1=x2;
27 x2=L+R-x1;
28 elseif fx1<fx2
29 R=x2;
30 x2=x1;
31 x1=L+R-x2;
32 elseif fx1==fx2

```

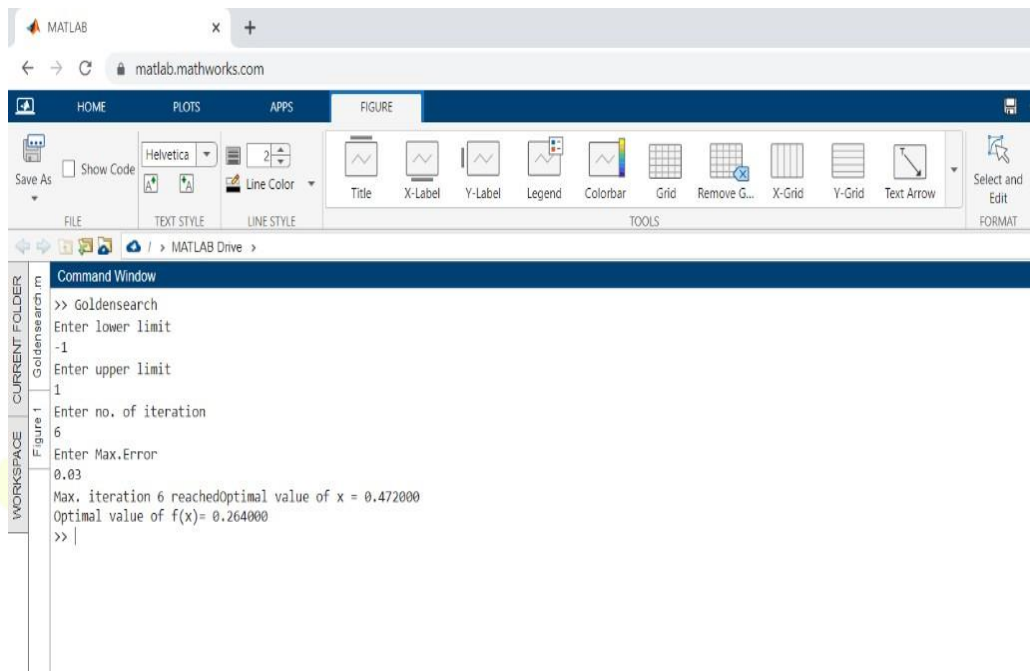


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New Open Save Go To Find Refactor Run Section Run and Advance Run Step Stop
FILE NAVIGATE CODE SECTION RUN
MATLAB Drive
Goldensearch.m
28 elseif fx1<fx2
29 R=x2;
30 x2=x1;
31 x1=L+R-x2;
32 elseif fx1==fx2
33 if min(abs(x1),abs(L))==abs(L)
34 R=x2;
35 else
36 L=x1;
37 end
38 end
39 if iter==n
40 break;
41 else
42 iter=iter+1;
43 end
44 end
45 % Display the condition met
46 if iter==n
47 fprintf('Max. iteration %d reached',n);
48 else
49 fprintf('Max. Error limit %f reached', maxerr);
50 end
51 % Printing the final results
52 Variables={'L','R','x1','x2','fx1','fx2'};
53 Res1=array2table(Res1);
54 Res1.Properties.VariableNames(1:size(Res1,2))=Variables;
55 % Compute & print optimal result
56 xopt=(L+R)/2;
57 fopt=f(xopt);
58 fprintf('Optimal value of x = %f\n',xopt);
59 fprintf('Optimal value of f(x)= %f\n',fopt);

```

GOLDEN SECTION SEARCH MATLAB CODING

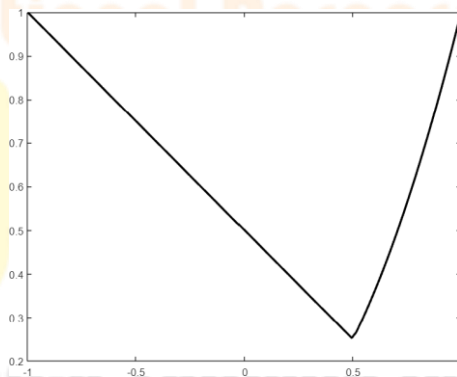
OUTPUT:


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MATLAB
x +
matlab.mathworks.com
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Save As Show Code Helvetica Line Color
FILE TEXT STYLE LINE STYLE TOOLS Select and Edit FORMAT
MATLAB Drive
Command Window
>> Goldensearch
Enter lower limit
-1
Enter upper limit
1
Enter no. of iteration
6
Enter Max.Error
0.03
Max. iteration 6 reached Optimal value of x = 0.472000
Optimal value of f(x)= 0.264000
>> |

```

COMMAND WINDOW OF GOLDEN SECTION SEARCH CODING

GRAPH OF GOLDEN SECTION SEARCH:

GOLDEN SECTION SEARCH GRAPH

CONCLUSION

Formalized the issue of safely reevaluating NLP calculations in distributed computing, and provided such a proposed model which satisfies info and result security. Such outcome confirmation instrument is incredibly effective and causes near zero extra expense on both cloud server and clients. Broad security investigation and analysis results show the prompt practicability of our plan.

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